

SRI SATYA SAI UNIVERSITY OF TECHNOLOGY & MEDICAL SCIENCES, SEHORE

# SYLLABUS M.SC MATHEMATICS – IV SEMESTER Functional Analysis-II MAT-401

# UNIT-I

Uniform boundedness theorem and some of its consequences, Open mapping and Closed graph theorems.

# UNIT-II

Hahn-Banach theorem for real linear spaces, Hahn-Banach theorem for complex linear spaces and Normed linear spaces.

# UNIT-III

Reflexive spaces, Hilbert spaces, Orthonormal Sets, Bessel's inequality, Complete orthonormal sets and Parseval's identity.

## UNIT-IV

Projection Mapping, Projection theorem structure of Hilbert spaces, Riesz representation theorem.

## UNIT-V

Adjoint of an operator on a Hilbert space, Reflexivity of Hilbert spaces, Self-adjoint operators, Positive operators, Projection, Normal and Unitary operators.

#### **Text Books:-**

- 1. E. Kreyszig, Introductory Functional Analysis with application, John Wiley and Sons New York.
- 2. G.F. Simmons, Introduction to Topology & Modern Analysis McGraw Hill, New York.

## **Reference:-**

1. B. Choudary and Sudarshan Nanda. Functional Analysis with application Wiley Eastern Ltd.

# M.Sc. (Mathematics) IV Semester Syllabus 2022-23



#### SCIENCES, SEHORE

## SYLLABUS M.SC MATHEMATICS – IV SEMESTER ADVANCED SPECIAL FUNCTION-II MAT-402

## UNIT-I

**Bessel function and Legendre polynomials :** Definition of  $J_n(z)$ , Bessel's differential equation, Generating function, Bessel's integral with index half and an odd integer.

## UNIT-II

Generating function for Legendre polynomials, Rodrigues formula, Bateman's generating function, Additional generating functions, Hypergeometric forms of  $P_n(X)$ .

#### UNIT-III

Special properties of  $P_n(X)$ , Some more generating functions, Laplace's first integral form, Othergonality.

#### UNIT-IV

Definition of Hermite polynomials  $H_n(X)$ ., Pure recurrence relations, Differential recurrence relations, Rodrigue's formula, Other generating functions, Orthogonality, Expansion of polynomials, More generating functions.

#### UNIT-V

**Laguerre Polynomials :** The Laguerre Polynomials  $L_n(X)$ . Generating functions, Pure recurrence relations, Differential recurrence relation, Rodrigo's formula, Orthogonal, Expansion of polynomials, Special properties, Other generating functions.

#### **Books :-**

- 1. Rainville E. D., Special Functions, the Macmillan Co., New York 1971.
- 2. Srivatava H.M., Gupta K.C. and Goyal S.P., The H- Functions of one and two variables with applications, South Asian Publication, New Delhi.
- 3. Saran N., Sharma S.D. and Trivedi , Special Function with application, Pragati Prakashan 1986.
- 4. The Saxena V.P., I-Function, Anamaya New Delhi, 2008.

#### **Reference Books:-**

- 1. Lebdev N.N., Sepcial Functions and Their Applications, Prentice Hall Englewood Cliffs, New Jersey, USA 1995.
- 2. Whittaker E.T. and Watson G.N., A Course of Modern Analysis, Cambridg University Press, London, 1963.

# M.Sc. (Mathematics) IV Semester Syllabus 2022-23



## SCIENCES, SEHORE

## SYLLABUS M.SC MATHEMATICS – IV SEMESTER Theory of Linear Operators-II MAT-403

## UNIT-I

Spectral properties of compact linear operators on normed spaces.

# UNIT-II

Behaviors' of Compact linear operators with respect to solvability of operators equation.

# UNIT-III

Fredholm type theorems, Fredholm alternative theorem, Fredholm alternative for integral equation, Spectral properties of bounded self – adjoint linear operator on complete hilbert space.

# UNIT-IV

Positive operators, Monotone sequence theorem for bounded self – adjoint operators on a complex hilbert space.

## UNIT-V

Square roots of a positive operator, Projection operators with applications.

#### **Books :-**

1. E. Kreyszig, Introductory Functional Analysis with application, John Wiley and Sons New York.

#### **Reference Book:-**

- 1. P.R. Halmos, Introduction to Hilbert space and the theory of Spectral Multiplicity, Second edition, Chelsea publishing co. N. Y. 1957.
- 2. N. Dundford and J.T. Schwartz, linear operator-3 part, Inter science/ Wiley, New York 1958-1971.
- 3. G. Bachman and L. Narci, Functional analysis, Academic press New York. 1966.



SRI SATYA SAI UNIVERSITY OF TECHNOLOGY & MEDICAL SCIENCES, SEHORE

## SYLLABUS M.SC MATHEMATICS – IV SEMESTER Integral Transforms-II MAT-404

# UNIT-I

Application of Laplace Transform to Boundary Value Problems.

# UNIT-II

Electric Circuits, Application to Beams.

# UNIT-III

The complex Fourier Transform, Inversion Formula, Fourier cosine and sine transform.

# UNIT-IV

Properties of Fourier, Transforms, Convolution & Parseval's identity.

## UNIT-V

Fourier Transform of the derivatives, Finite Fourier Sine and Cosine Transform, Inversion Operational and Combined properties of Fourier transform.

#### Books :-

1. L. K. Vashisht ,Integral Transform, Krishna's Educational Publisher's India.

#### **Recommended Books :-**

1. J. K. Goyal and Gupta ,Integral Transform, Pragati Prakashan India.



# SCIENCES, SEHORE

## SYLLABUS M.SC MATHEMATICS – IV SEMESTER Spherical Trigonometry and Astronomy-II MAT-405

## UNIT-I

Spherical Astronomy - Various system of references and related topics.

# UNIT-II

Celestial sphere.

# UNIT-III

Transit instrument.

## UNIT-IV

Atmospheric Retraction.

## UNIT-V

Time planetary phenomena

#### **Books :-**

1. W. M. Smart ,Textbook on Spherical Astronomy, Cambridge University Press.

#### **Recommended Books :-**

1. G. S. Malik , Spherical Astronomy, Kedar Nath Ram Nath Publication India .



## SCIENCES, SEHORE

## SYLLABUS M.SC MATHEMATICS – IV SEMESTER Dissertation MAT-406

- A Dissertation on any research topic of Mathematics such as:
  - 1. Graph theory
  - 2. Probability (Discrete and Measure-theoretic)
  - 3. Analysis (real and functional)
  - 4. Algebra (linear and abstract)
  - 5. Fixed point theory
  - 6. Fuzzy sets, and Fuzzy logic
  - 7. Operational Research
  - 8. Numerical Methods
  - 9. Mathematical modeling
  - 10. Data Mining